
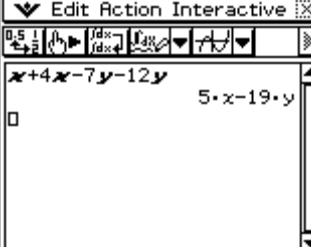


Algebra-Classpad-Examples

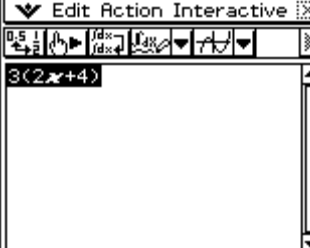


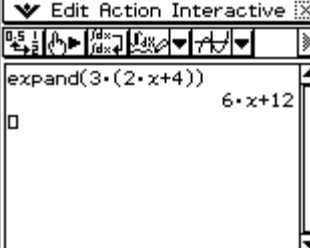
Simplifying Algebraic expressions

How do we simplify algebraic expressions

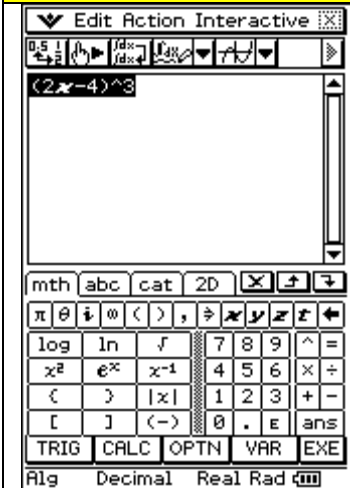
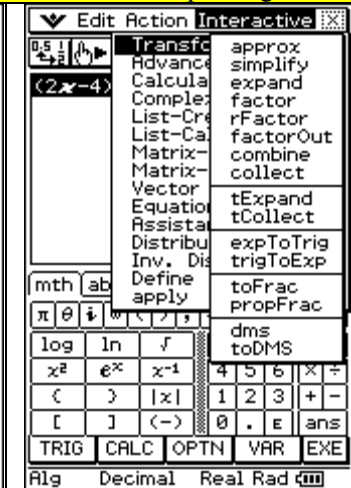

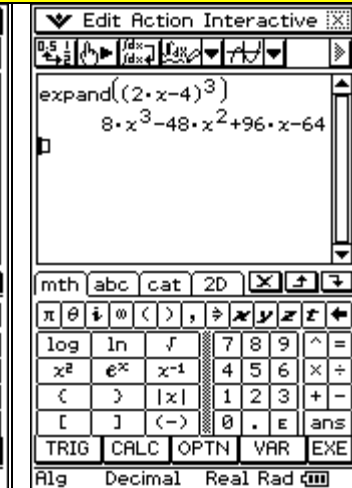
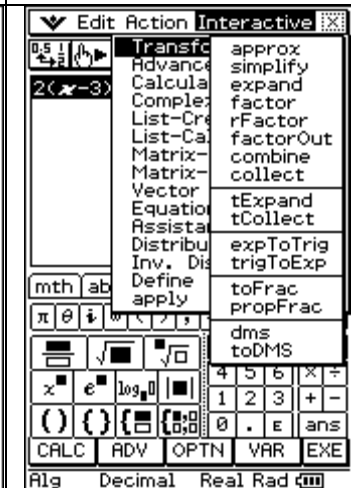


			
<p>Go to Main and enter the screen And enter the algebraic expression <math>x + 4x - 7y - 12y</math> Press EXE</p>	<p>And you get the answer</p>		

Expanding expressions

How do we expand expressions


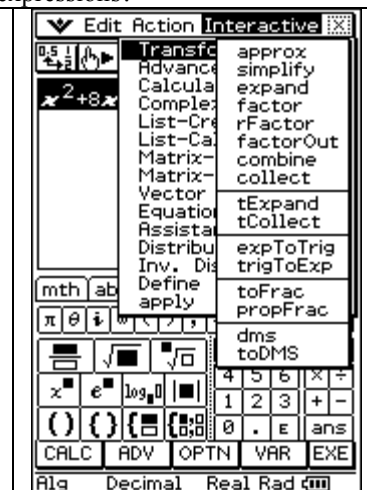
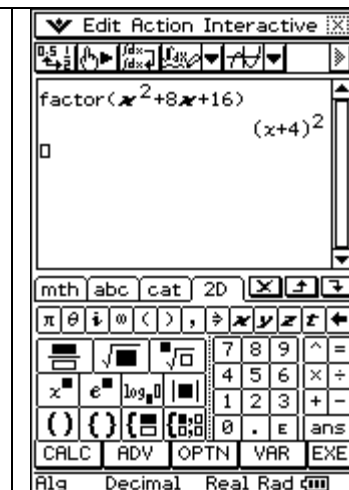
			
<p>Go to main screen and enter <math>3(2x + 4)</math> Highlight it</p>	<p>Tap Interactive Transformation Expand</p>	<p>Just press OK and you will get the answer</p>	<p>The answer is shown</p>

## Expanding more difficult expressions

			
<p>Go to main screen again Enter the following expression <math>(2x - 4)^3</math> Highlight it</p>	<p>Go to Interactive Transformation Expand again</p>	<p>Just press Ok</p>	<p>And the answer is given for us once again</p>
			
<p>This time lets repeat it using a more complicated expression Go to Main and enter the following <math>2(x - 3)^3 - 5(x + 2)^2</math> Highlight it once again</p>	<p>Tap Interactive Transformation Expand</p>	<p>Press OK</p>	<p>And the answer is worked out for you.</p>

## Factorizing

How do we factorize algebraic expressions?

		
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Go to main screen again and enter the following

$$x^2 + 8x + 16$$


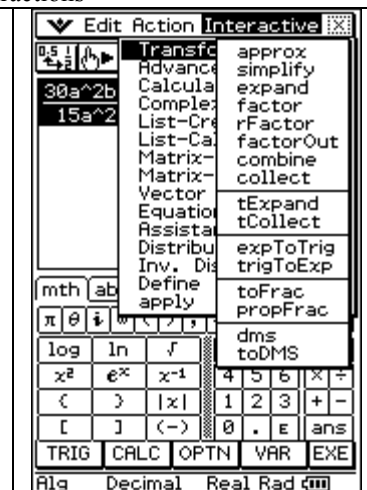
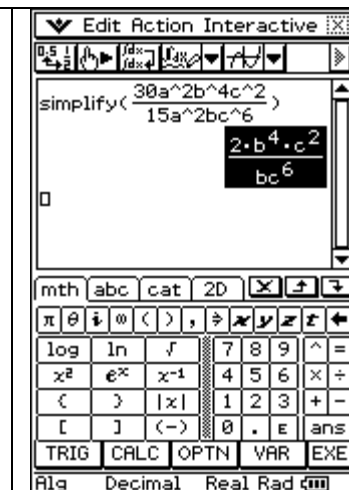
Highlight it

Go to Interactive Transformation factor

And the answer is shown for us

## Simplifying algebraic fractions

How do we simplify algebraic fractions

		
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Go to main screen and enter

$$\frac{30a^3b^4c^2}{15a^2bc^6}$$

You will need to use 2D and fraction template Highlight it

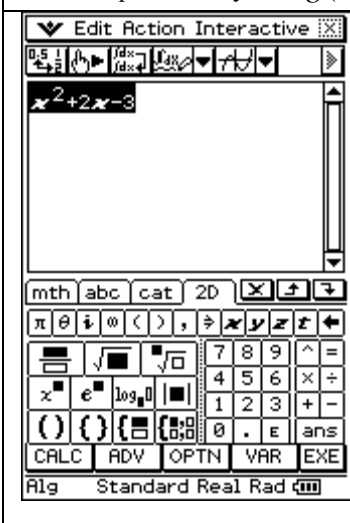
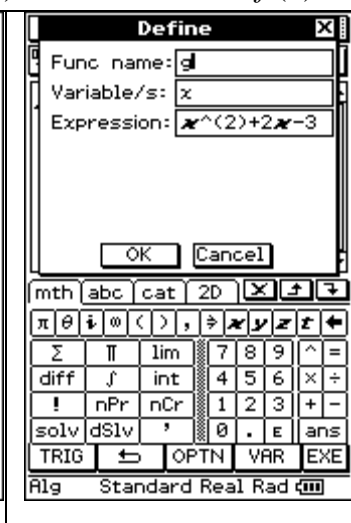

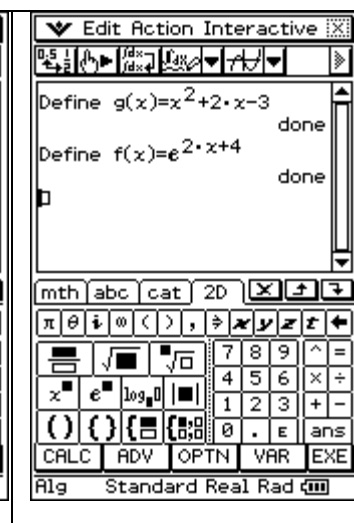
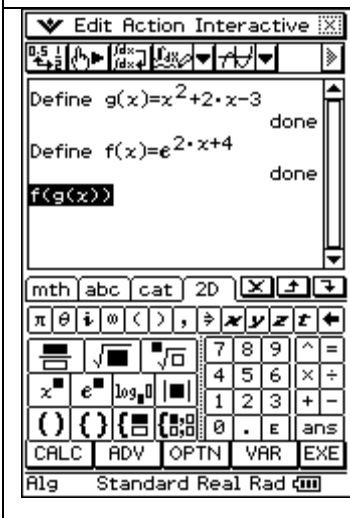
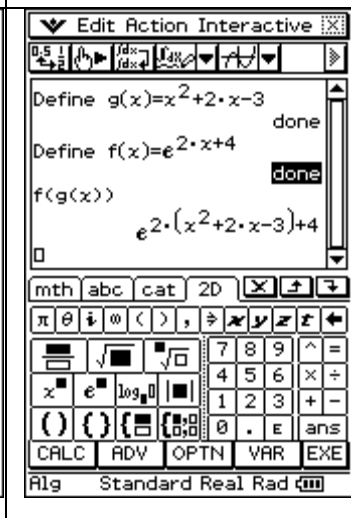
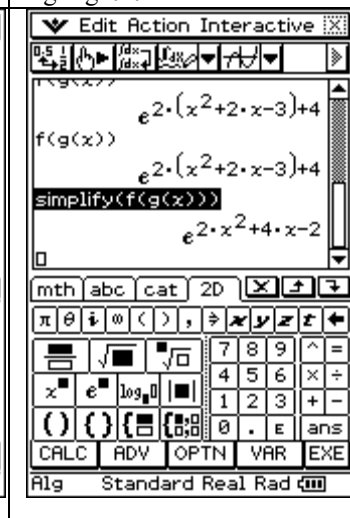
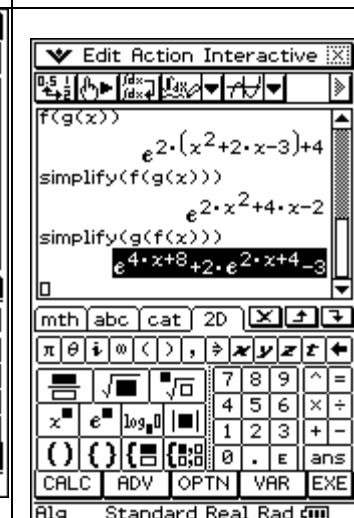
Tap Interactive Transformation Simplify

And the answer is given. I have highlighted the answer



How do we calculate a composite function?

For example let's say that  $g(x) = x^2 + 2x - 3$  and  $f(x) = e^{2x+4}$ . Find  $f(g(x))$

			
<p>First enter the equation of <math>f(x)</math> into the main section and highlight it</p>	<p>Press interactive Then define-call it <math>g(x)</math> Press OK</p>	<p>This is what we see when we press OK, now repeat it for <math>f(x)</math> Enter the equation- and highlight it</p>	<p>Go to interactive Define Call it <math>f(x)</math></p>
			
<p>Now we enter the function we need to work out</p>	<p>And the answer is on the screen above But we can use the power of the calculator to simplify the answer</p>	<p>We can use the power of the calculator to simplify our answers by Highlight it Interactive Transformation Simplify</p>	<p>We can do the same with <math>g(f(x))</math> So we enter the equation and then go Interactive Transformation Simplify And we get the highlighted answer</p>

## Finding the inverse function

For the function  $h(x) = 1 + e^{-x}$ , find the inverse function  $h^{-1}(x)$

Put  $x = 1 + e^{-y}$  and then select this input

Tap interactive  
Then equation  
Then solve

In the variable replace it with y instead

Press ok and the inverse function is calculated

## Solving equations exactly

Solving equations- exact

Find the solution set for the equation  $e^{4x} - 5e^{2x} + 4 = 0$

Enter the equation in the main application screen. And then highlight it

Tap interactive  
Equation  
Solve

Make sure Solve is selected as this will give us exact values



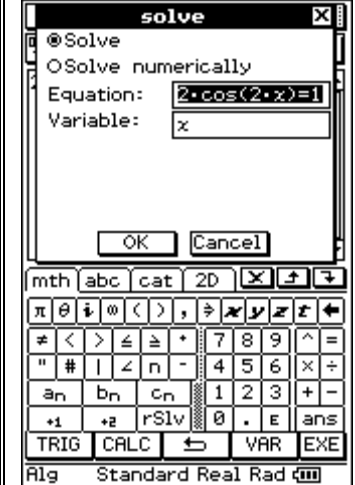
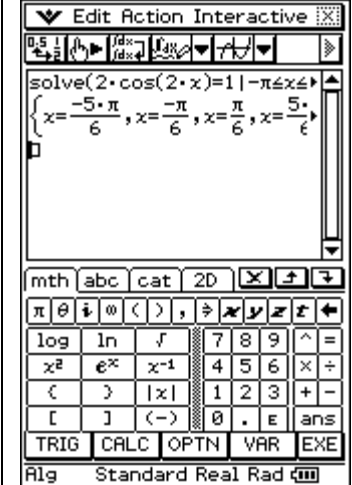
Sometimes it is not possible to get exact answers to all questions, so it would be better to select solve numerically.  
Notice we do not obtain all the solutions!

## Solving equations exactly- within a given domain

Solving equations , exactly

Find the exact values for the solutions to equations within a given domain.

Find the exact values of  $x \in (-\pi, \pi)$  such that  $2 \cos(2x) = 1$ 

			
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Type the equation above into the main section of the calculator

Go to OPTN and enter the domain  
Then press interactive  
Equation  
Solve

We obtain the various solution for our question

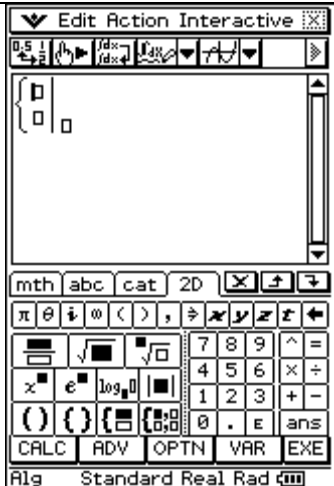
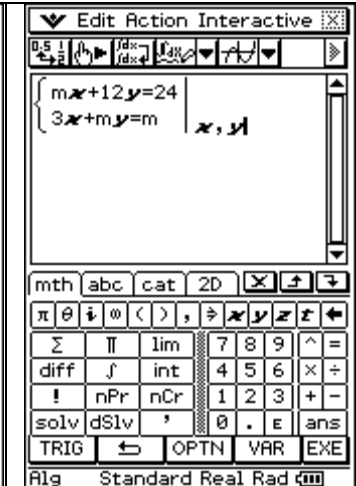
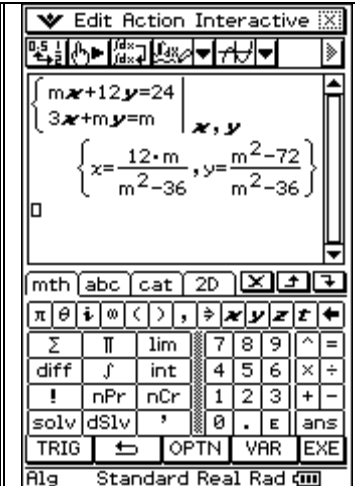
## Simultaneous Equations

How do we find the solution to simultaneous equations?

$$mx + 12y = 24$$

Find the solution to the following equations

$$3x + my = m$$

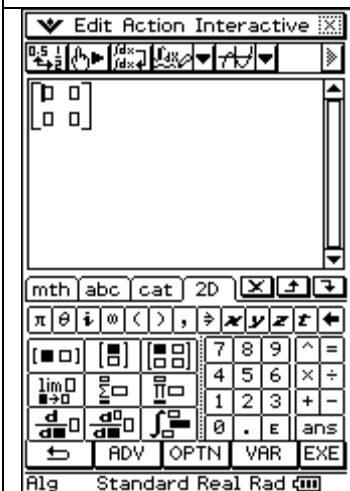
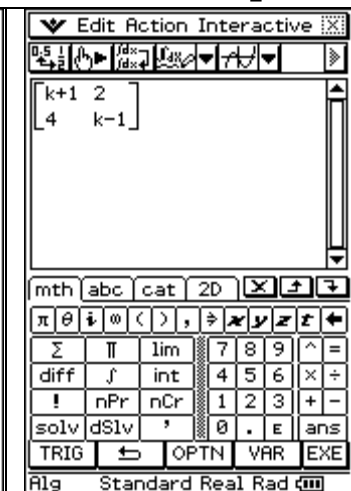
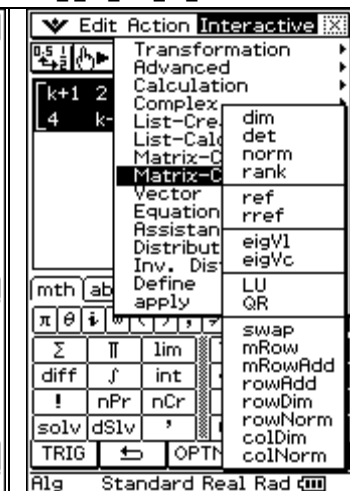
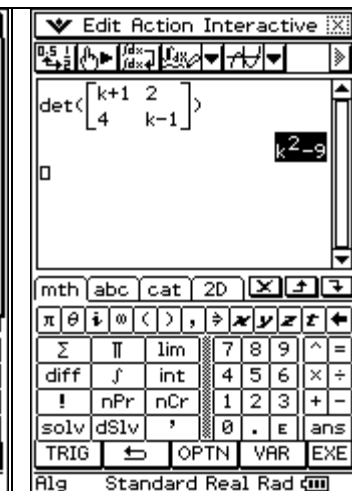
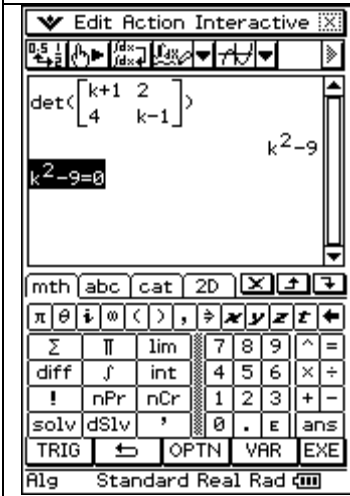
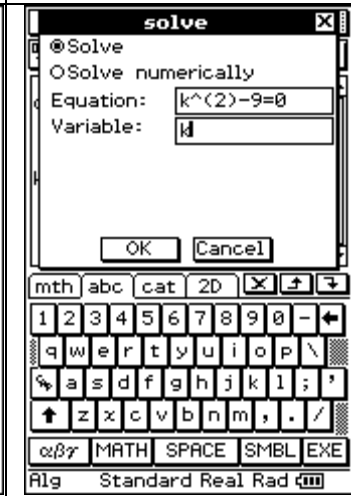
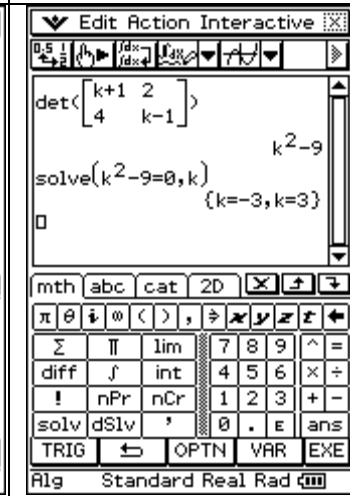
			
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Go to main area  
Go to 2D and select the appropriate templateNow enter the information from the equations above.  
**Be careful of order x and y in the equations.**Now press EXE  
And we have solved the simultaneous equations.

## Equations and Matrices

Determining when a system of equations has a unique solution

Consider the linear equations given by the following:  $\begin{bmatrix} k+1 & 2 \\ 4 & k-1 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 0 \\ k \end{bmatrix}$ , find value of k for a unique solution

			
<p>Go to Main area and use 2D and use Matrix template</p>	<p>Now enter the information carefully. Remember to use abc keys</p>	<p>Now select the matrix and Go interactive Matrix-calculation det</p>	<p>This is what you will obtain</p>
			
<p>Select the expression for the determinant and put it onto a new line and set to zero and solve</p>	<p>Highlight it Interactive Equation Solve Remember to put k for variable</p>	<p>And we get the answers. This tells us when the system of equation does not have a unique solution. For all other values of k it will have a unique solution</p>	

Solving linear inequalities

How do we solve linear inequalities such as  $4 - 5x > 9$

<p>Once again enter the information into the calculator</p>	<p>Go to interactive Equation Solve</p>	<p>And the solution is provided for us.</p>	

Solving simultaneous linear equations -2

How do we solve simultaneous equations using the classpad  
For example we want to solve the following

<p>Go to main screen Then go to 2D and use the template and you will see the above</p> <p>If it 3 equation tap on it and it will have three fields to put information in</p>	<p>Then input the information  Put the information in carefully and then type in EXE</p>	<p>And the answer is given for us</p>	

## Rearranging equations

We want to rearrange the following equation

Make a the subject in the equation  $t = 2a + 5b$

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Type the equation into the main section

Interactive  
Equation  
Solve

Make sure the variable is a

And the answer is above


## Graphing

Many ways to graph using the classpad but let us use one method.

We want to graph the graph of  $3x + 2y = 12$

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Firstly type the equation in the main window

Now press the graph button  
  
 And you will see the following

Now drag the highlight equation into the window below

Resize the bottom window to see the graph better

<p>To locate the horizontal intercept Tap Analysis G-Solve Root Notice the answer is x =4</p>	<p>To locate the vertical intercept Tap- Analysis G-Solve y-intercept Notice answer is y - 6</p>		

Graphing Parabola Features


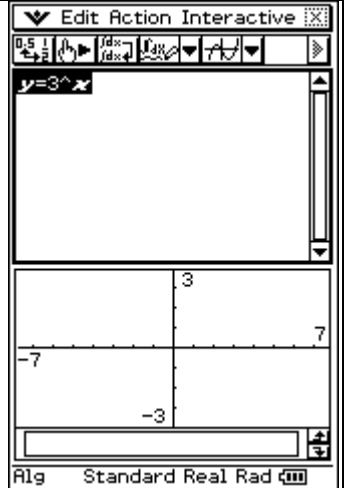
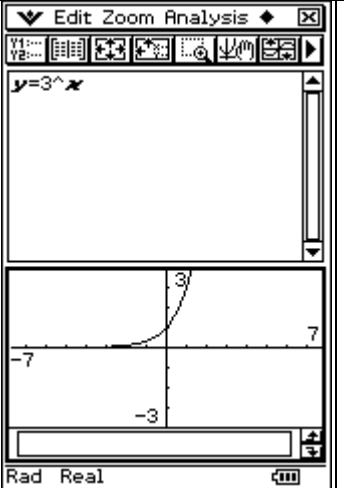
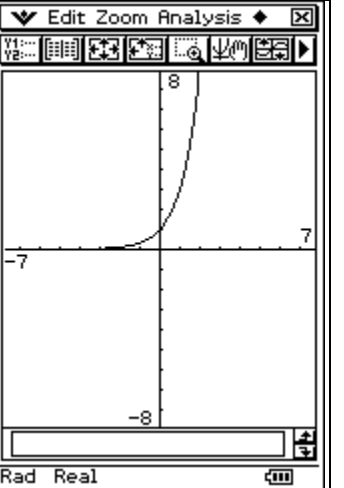
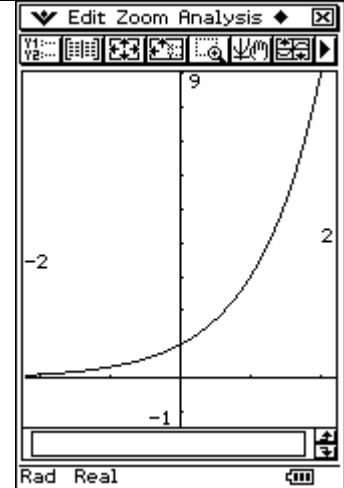
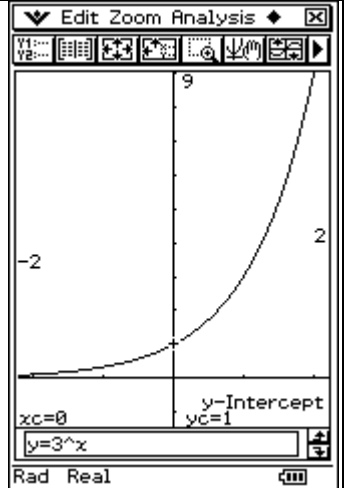
Lets us plot a parabola and analyse some of its features  
The graph of  $y = x^2 + 3x - 4$

<p>Put the graph into the main screen quickly</p>	<p>Tap the graph button</p>	<p>Highlight the graph and drag it into the scene below</p>	<p>Now resize the bottom screen to see the graph better</p>

Horizontal intercepts Tap- Analysis G-Solve Root Use left and right cursor to move to each intercept	Vertical intercept Go Analysis G-Solve y-intercept	Vertex Go Analysis G-Solve Min	
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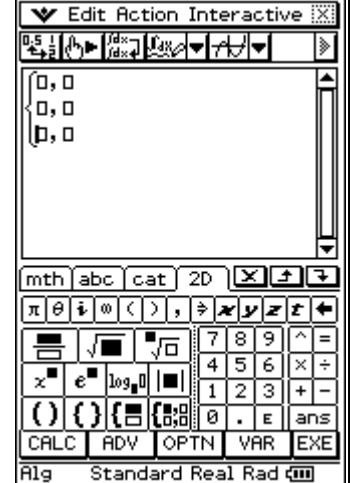
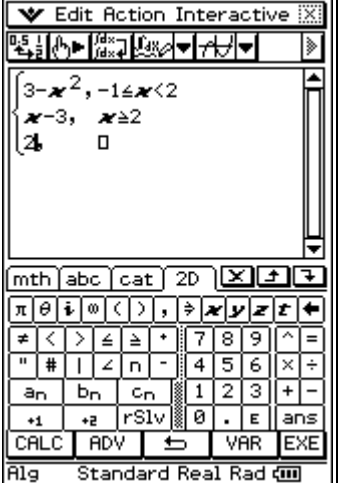
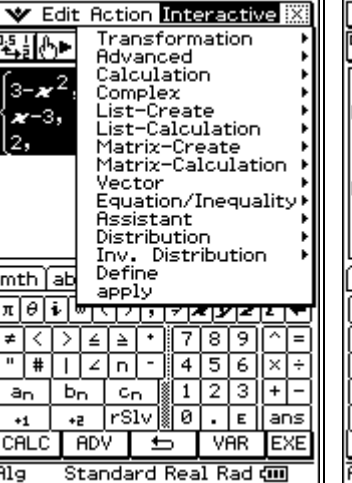
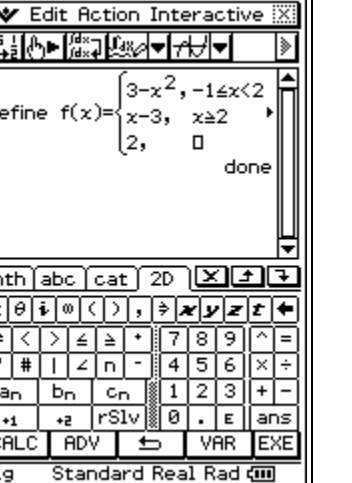

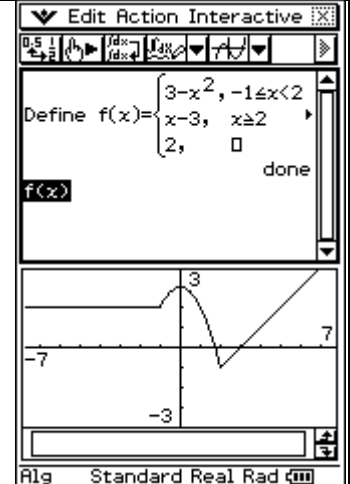
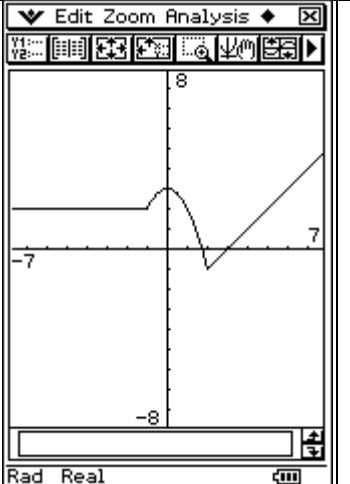
Graph of an Exponential function

How do we graph exponential  $y = 3^x$

			
Go to the main menu and type the equation out as follows	Press the graph button and then highlight the graph	Drag it into the graphing window	Make the window of the bottom screen bigger
			
To get a better picture Go to Zoom Quick $e^x$	To locate vertical intercept Tap- Analysis G-Solve y-Intercept		

### Piecewise Defined functions

Imagine we want to do piecewise defined function such as the following:  $f(x) = \begin{cases} 3-x^2 & -1 \leq x \leq 2 \\ x-3 & x > 2 \\ 2 & \text{elsewhere} \end{cases}$


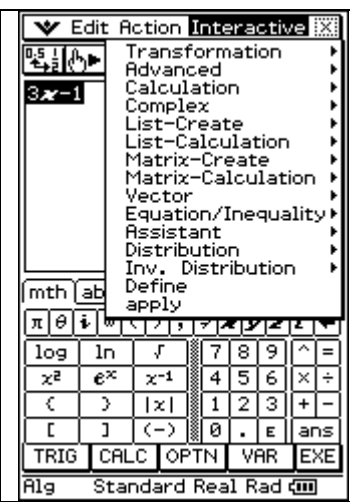
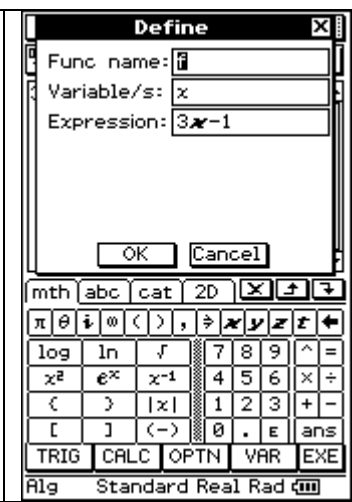
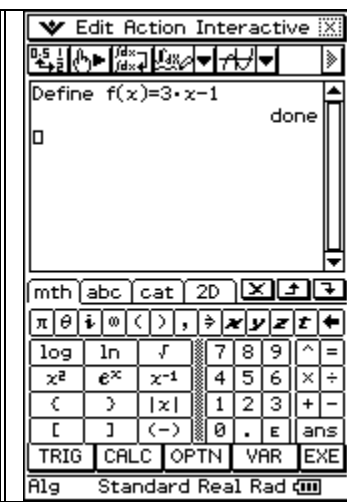
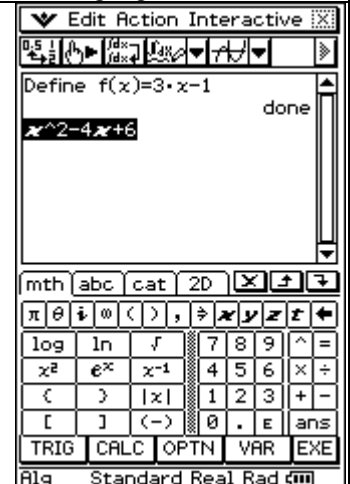
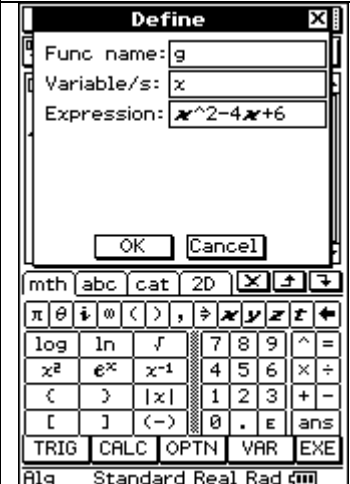
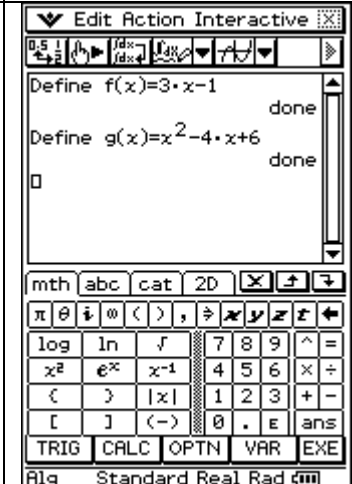
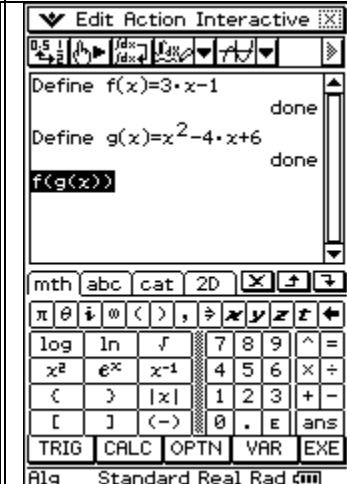
			
<p>Go to main screen Go to 2D tab</p> <p>Tap twice on the </p> <p>You will create three empty rows</p>	<p>This is what we see</p> <p>Now highlight it</p>	<p>Now we can define it</p> <p>Highlight it Interactive Define Call it f</p>	<p>This is what we see now we can press the graph button</p>
			

## Composite Functions

How to we do composite functions and graph them

$$f(x) = 3x - 1 \text{ and the } g(x) = x^2 - 4x + 6$$

Find  $f(g(x))$  and graph it

			
<p>First we need to go to main section and type in the equation and define it We do that one at a time Type- <math>3x - 1</math> Then highlight it and define it</p>			
			
<p>We repeat the same above process for the other equation <math>x^2 - 4x + 6</math></p>		<p>So we have defined the two equations now all you have to do is Write <math>f(g(x))</math></p>	

<p>Press EXE And that is the answer</p>	<p>We can draw it, of course we have not defined the range or the domain of the composite function</p>	<p>Resize the function so we can see the entire screen.</p>	<p>Go to zoom Quick x^2 to get it the graph to look better on the screen</p>

Jump to an exact coordinate in a graph at a particular point- x-CAL or y-CAL

Using the example from before we can find the value of y for any particular value of x

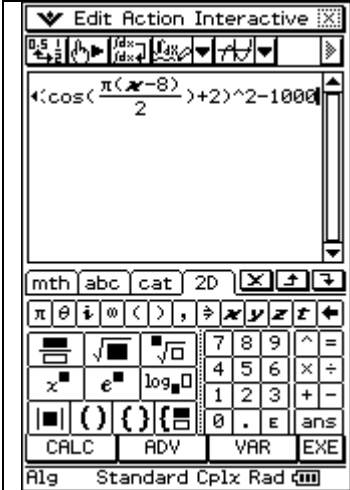
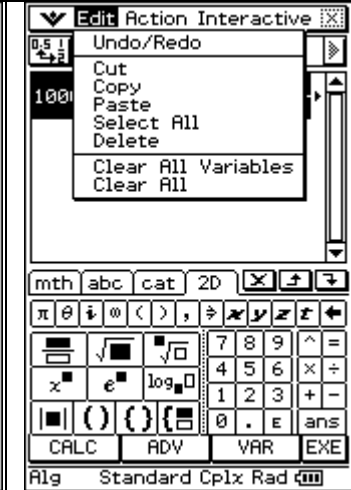
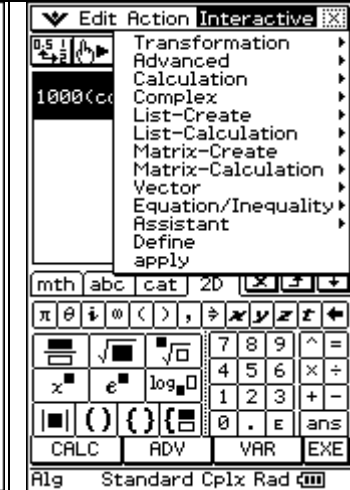
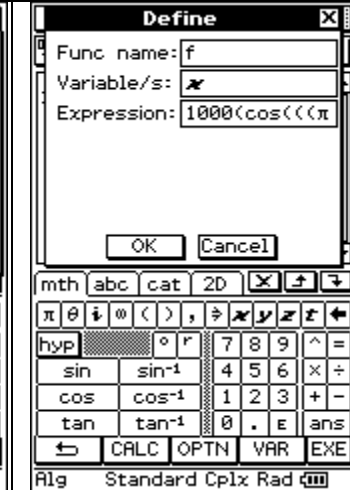
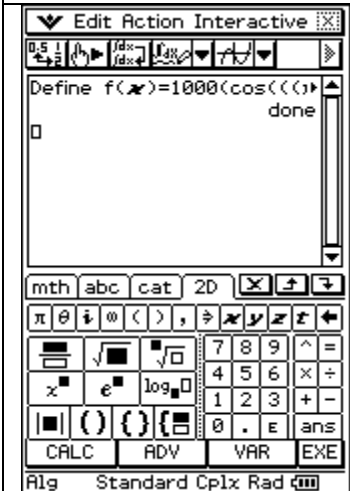
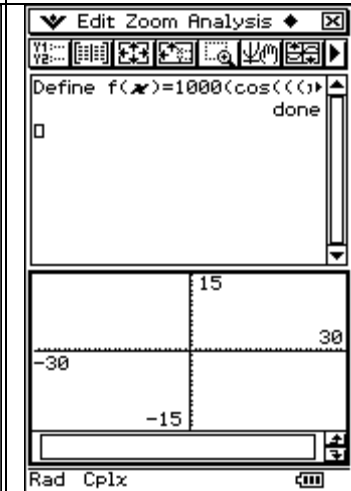
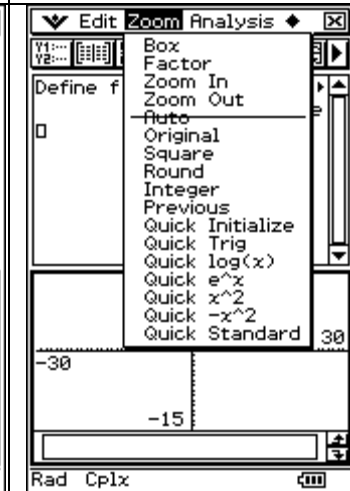
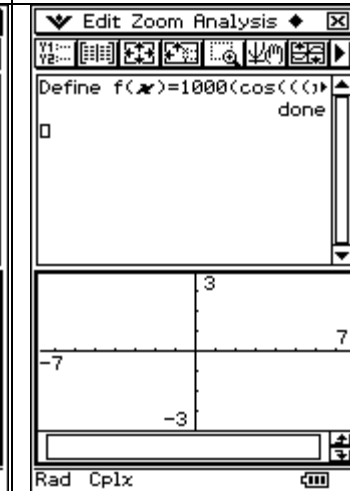
<p>Using the graph from the previous example</p>	<p>Press 1 in the graph screen</p>	<p>Enter 2.5</p>	<p>Press Analysis G-Solve Then y-Cal We put the value for x</p>
<p>Put x = 2</p>	<p>And the answer is y = 5</p>	<p>Analysis G-Solve The n x-Cal Now enter y = 3</p>	<p>So we get x = -3.645</p>

## Graphs-function-classpad-examples

## Sketching Graphs

Sketch the following graph

$$f(x) = 1000 \left( \cos \left( \frac{\pi(x-8)}{2} \right) + 2 \right)^2 - 1000 \quad 8 \leq x \leq 16$$

			
<p>Step-1-Put the function into the main window of calculator</p>	<p>Step-2-Select the function ,select edit and then select all to select the entire function</p>	<p>Step-3- Now go to interactive and tap on define</p>	<p>Step-4-Now we define the equation by calling it</p>
			
<p>Step-5-Once you press OK from the previous step this is what you will see. Notice we have defined the equation with the symbol <math>f(x)</math></p>	<p>Step-6- Tap the graph image which will open a graph window in the bottom half of the screen</p>	<p>Step-7-Tap Zoom Quick Initialize It set the screen</p>	<p>Step-8- This is what you will see when you have pressed zoom quick initialize</p>

<p>Step-9- Now select <math>f(x)</math></p>	<p>Step-10-Drag it into the graph window and this is what you will see</p>	<p>Step-11- Press  and set the window setting. Use the domain information</p>	<p>Step-11- Press Zoom Auto and select full resize window and this is what you will get</p>

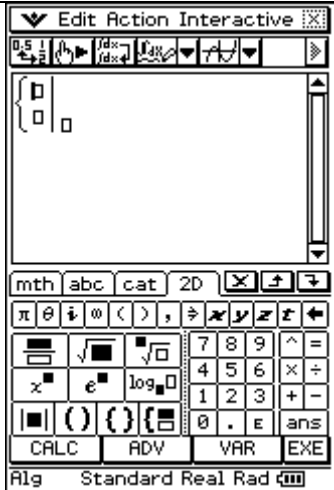
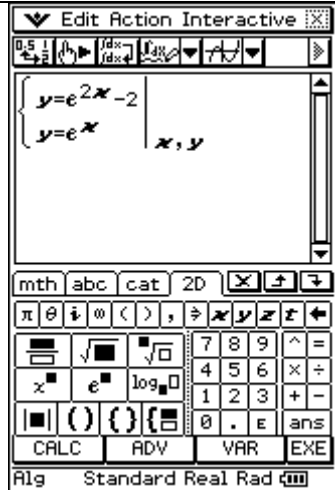
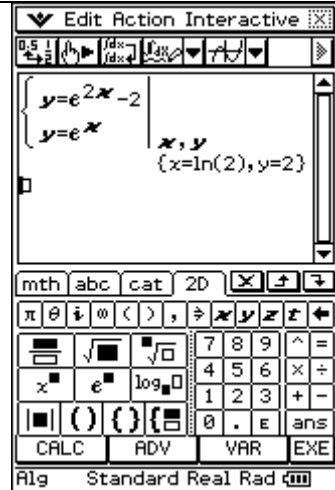
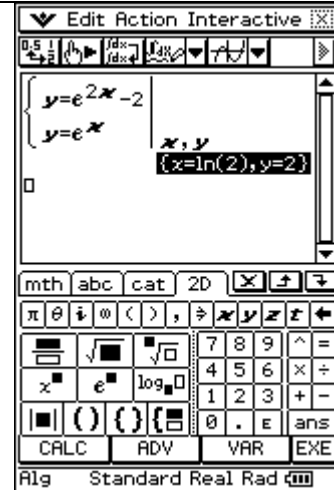
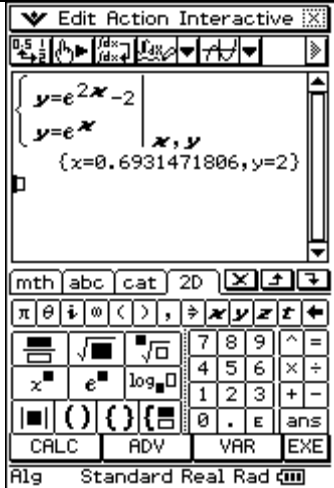
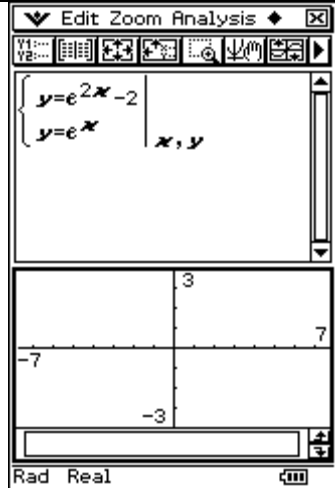
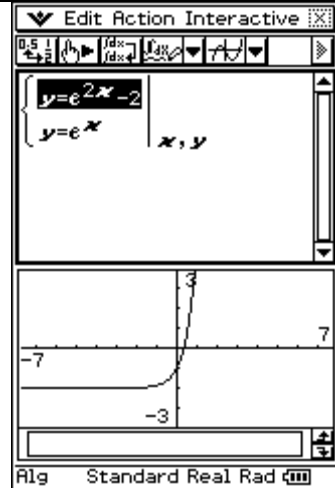
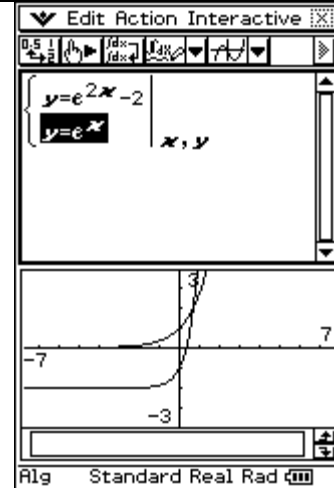
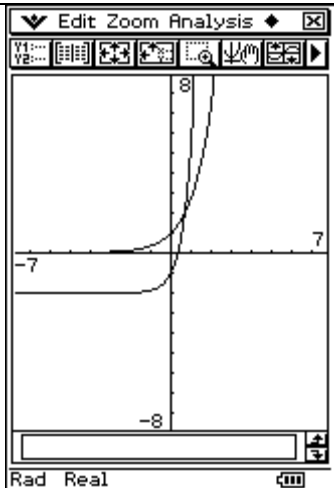
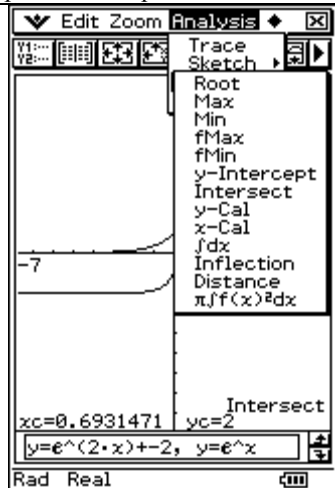
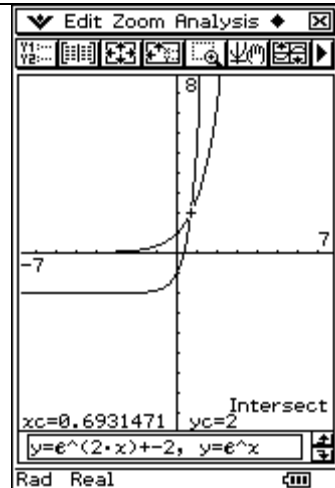

Finding exact values for a particular function

Finding the exact values of the above function how do we do it. For example how do we find  $f(x) = 1250$ ,  $8 \leq x \leq 16$

<p>Step -1- Set <math>f(x)=1250</math></p>	<p>Step-2- Now highlight this expression by pressing Edit and select all</p>	<p>Step-3- Press interactive and then equation and then solve</p>	<p>Step-4- This is what you will see when you press solve Now press OK</p>
<p>Step-5- This is what you will see which does not make any sense does it?</p>	<p>Step-6- Put <math> 8 \leq x \leq 16</math> before the ,x</p>	<p>Step-7- see the graphical solution by typing 1250 and dragging them into graph window</p>	<p>Step-8- Make it full window</p>


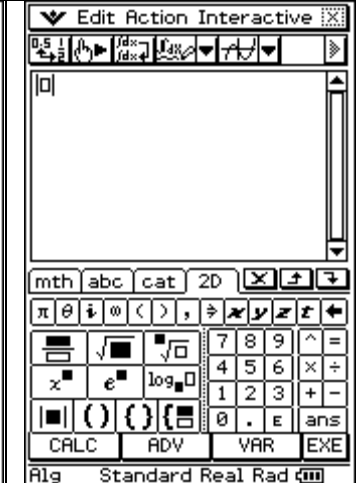

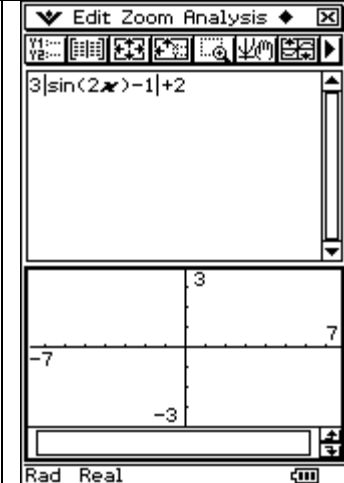

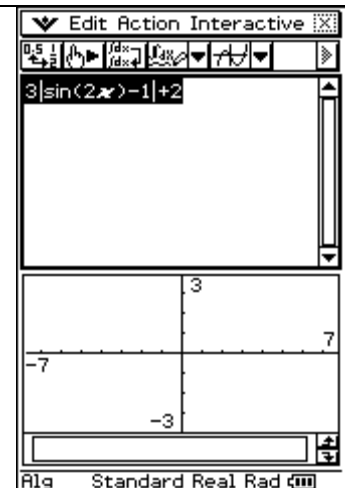
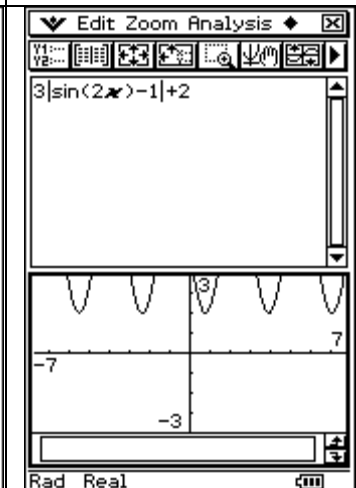
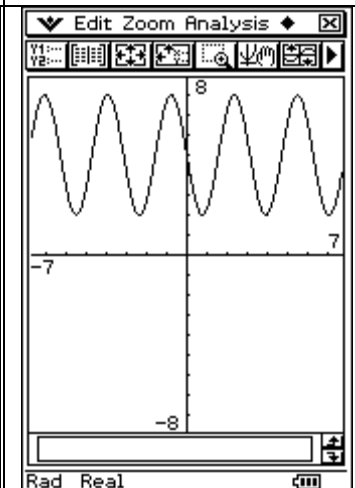
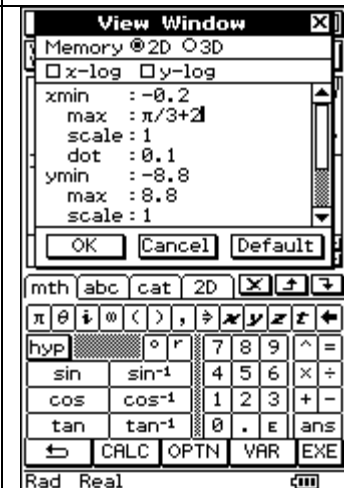

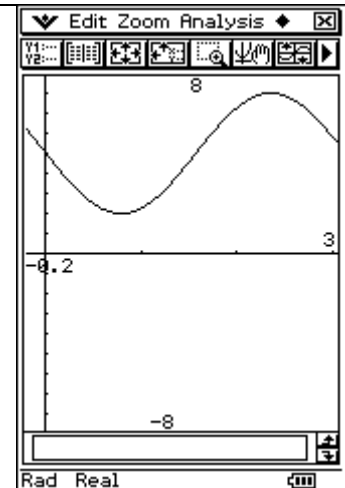
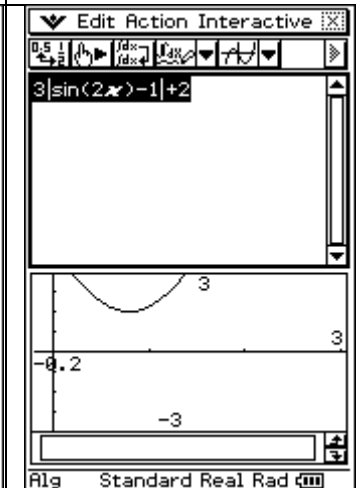
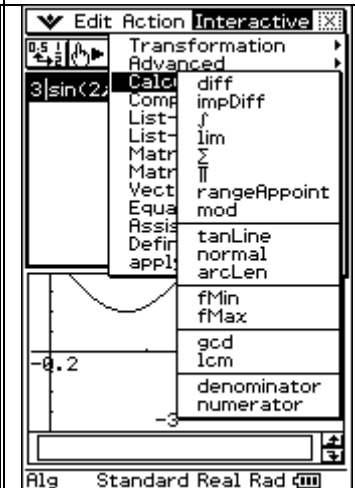
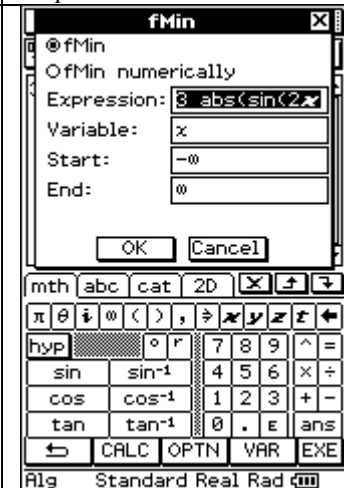
### Finding the intersection point of two graphs exactly.

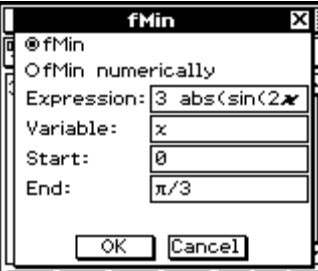
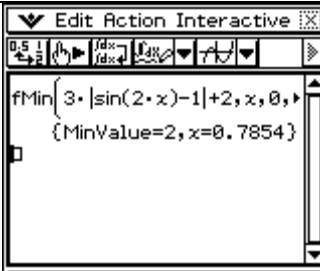
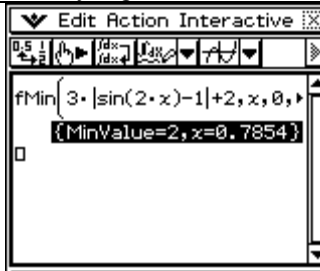
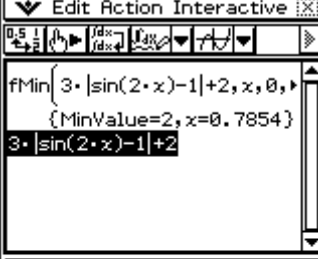

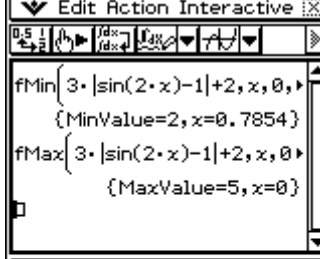
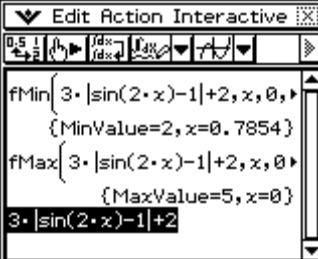
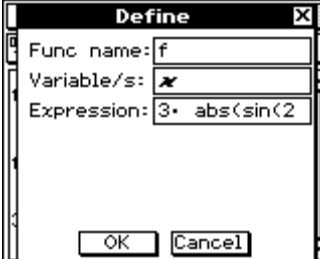
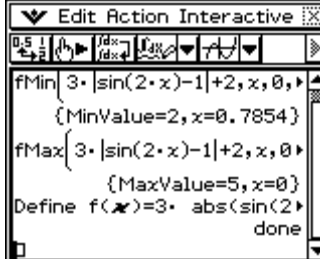
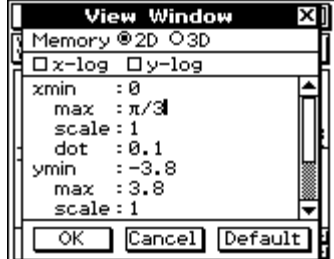
Finding the intersection between two graphs  $f(x) = e^{2x} - 2$  and  $g(x) = e^x$

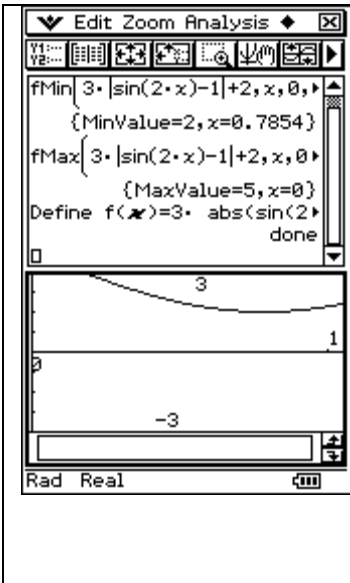
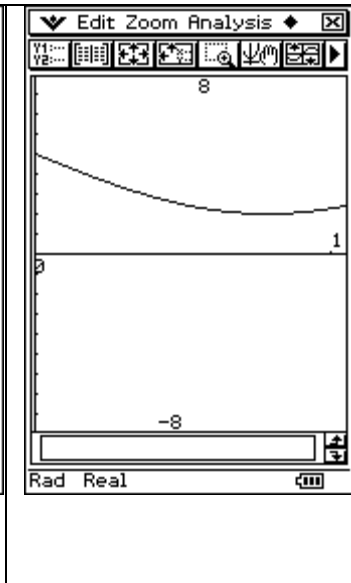
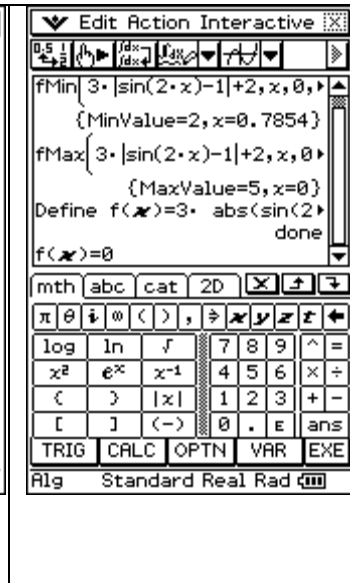
			
<p>Press 2D and then Press simultaneous template</p>	<p>Enter the information very carefully</p>	<p>Press EXE gives the following screen above</p>	<p>Press <math>\frac{0.5}{1}</math> will give us the decimal equivalent First you must highlight it</p>
			
<p>Now press <math>\frac{0.5}{1}</math> will give us the decimal equivalent</p>	<p>To sketch the graphs you can open the split screen Tap the graph screen and press zoom-quick initialize</p>	<p>Now drag top graph into screen below And this is what you will see above</p>	<p>Now drag the other graph</p>
			
<p>Now select the resize screen to make the graph take up the entire screen</p>	<p>Press Analysis G-Solve Intersect</p>	<p>You will get the following</p>	<p>Notice where the graphs intersect <math>x = 0.69</math> and <math>y = 2</math></p>

## Finding the minimum and maximum values in exact format

Find the range of the function  $f : \left[0, \frac{\pi}{3}\right] \rightarrow \mathbb{R} \quad f(x) = 3|\sin(2x) - 1| + 2$

			
<p>Make sure you set Alg, Standard, Real and Rad mode first</p>	<p>Now enter the equation very carefully Use 2D for the brackets</p>	<p>Put the equation in</p>	<p>Tap the graph  which will open the graph window in the bottom half</p>
			
<p>Now highlight the graph and drag it into the graph window</p>	<p>This is what you see. You might have to press ZOOM Quick Initialize</p>	<p>Now press the resize option</p>	<p>Press  to enter the domain information. Good to choose values just outside the value so you can see if the max or min occurs at the endpoints</p>
			

<p>Press OK gives the above</p> 	<p>Select the function and go to interactive-calculation-fMin</p> 	<p>This is the screen you will see before you press fMin</p> 	<p>Now enter the start and the ending values</p>
<p>We have entered the start and the end values and we press OK</p>	<p>This is what we obtain once we press OK So the MinValue = 2 at x = 0.7854</p>	<p>Press the decimal to exact button once you have highlighted the value gives</p>	<p><b>CAUTION</b> fMIN and fMAX will only return ONE VALUE for a minimum or maximum even if there are other values.  So if the function repeats itself then we will need to use another method.</p>
			
<p>Highlight the function and go through the entire process</p>	<p>Put the values in and press OK</p>	<p>This is what we obtain</p>	<p>So the range is [2,5]</p>
			
<p>Step-1-The other method-highlight the equation and we will define it</p>	<p>Step-2-Define it by calling it f</p>	<p>Step-3-Press OK</p>	<p>Step-4-Adjust the domain again</p>

			
Step-5-Press OK	Step-6-Press resize for graph	Step-7-Now we want to find the derivative of f and set it to zero to find the values of the minimum	Highlight it and go

How do I find the minimum or max value of a function for all real values of x if exact values are required

Find the value of x that minimizes the following function

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Enter the equation into the main screen  
Highlight the equation to define it

Press Define and you will get the following

Define it by calling it f

So this is the screen we get once we have defined the equation.

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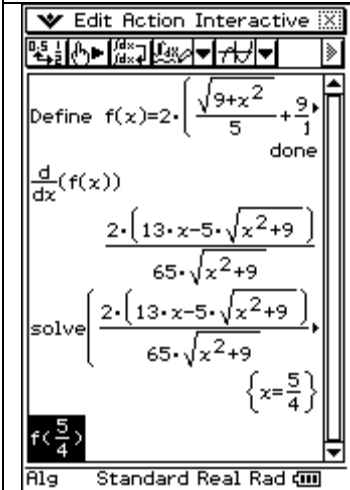
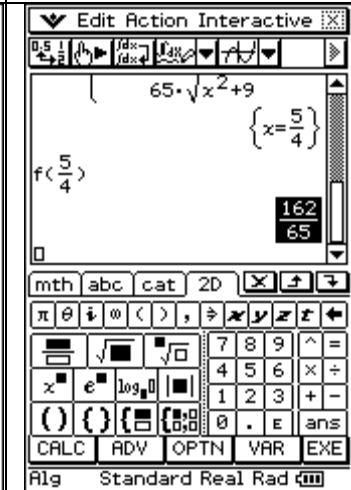
Write f(x)

Now open graph screen to see what the graph looks like  
Press the graph symbol

Now tap on the graph screen to zoom –quick initialize and then drag f(x) into the graph section

We can use the graph to find the minimum  
Press analysis  
G-Solve  
Min  
And we will get the minimum in decimal  
But we want exact?



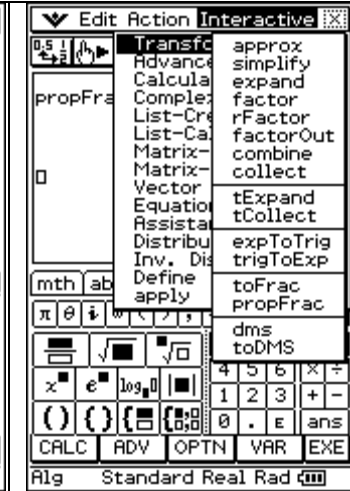
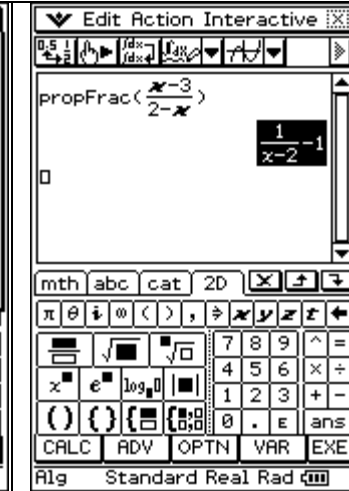
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<p>Go back and highlight f(x) and then</p>	<p>Go interactive Calculate Diff</p>	<p>Now drag this function and set it to zero and solve the equation</p>	<p>We get the precise value for the minimum which is <math>\frac{5}{4}</math></p>
			
<p>Now write <math>f(\frac{5}{4})</math> and let the calculator find the y value or f(x)</p>	<p>Press EXE And we have obtained the answers in exact form</p>	<p>So the exact values are <math>x = \frac{5}{4}</math> and <math>y = \frac{162}{65}</math></p>	

Sketching rational functions and showing asymptotes

Sometimes we are given a function and we can see that it possibly has an asymptote but it is not in the usual form so what can we do?

Put the following into an easier form to recognize its asymptotes -  $f(x) = \frac{x-3}{2-x}$


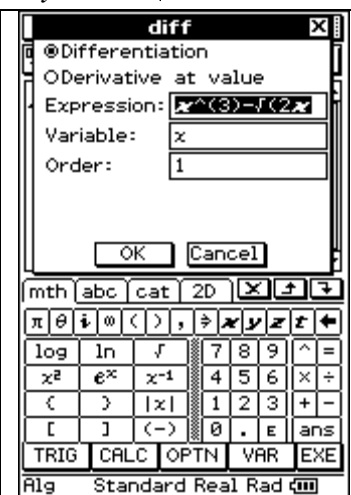
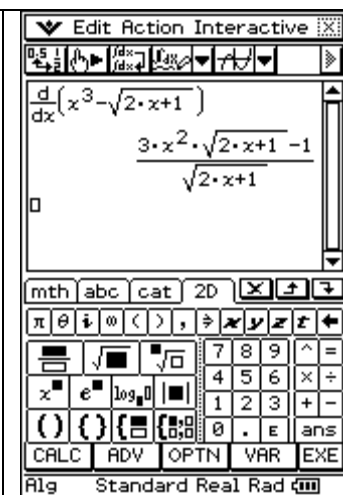
			
<p>Go to Main section and then go 2D and select the fraction mode and put the equation in</p>	<p>Highlight the function</p>	<p>Tap –interactive Transformation propFrac</p>	<p>This is what you will get</p>
<p>And it is easy to see that we have two asymptotes one at X =2 and y = -1</p>			

## Calculus-Classpad-Examples

## Finding the Derivatives of given functions

How do I find the derivative of a particular function?

Find the derivative of the function  $y = x^3 - \sqrt{2x+1}$

		
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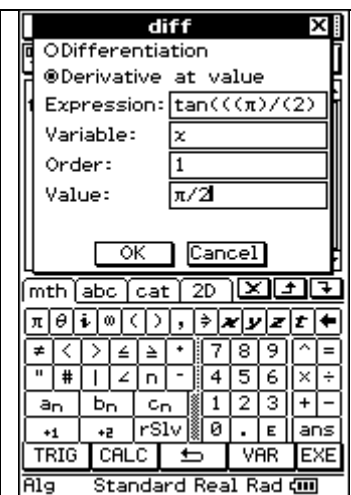
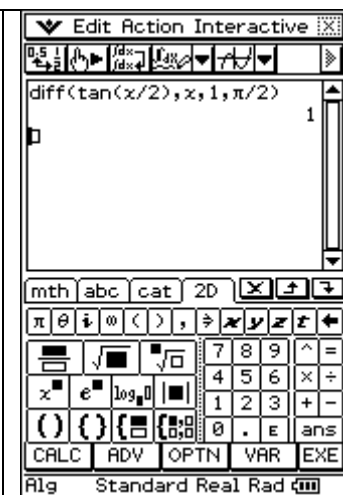
Enter the function into the main window of the calculator and highlight it

Tap interactive  
Calculation  
Diff  
Press OK when you get the following

And that is your answer there

## Derivative at a particular point

Say we want to find the derivative of the function  $f(x) = \tan\left(\frac{x}{2}\right)$  and we want to find the derivative  $f'\left(\frac{\pi}{2}\right)$

		
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Enter the equation in the main window and highlight once again.

Remember to use the 2D

section to input the  $\frac{x}{2}$



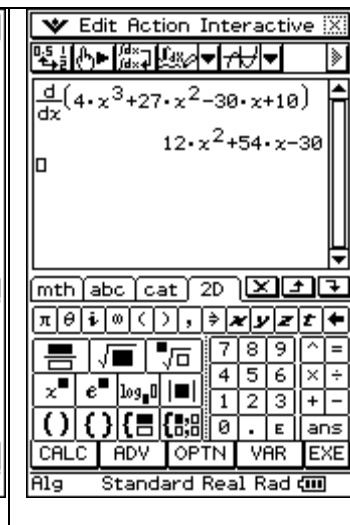

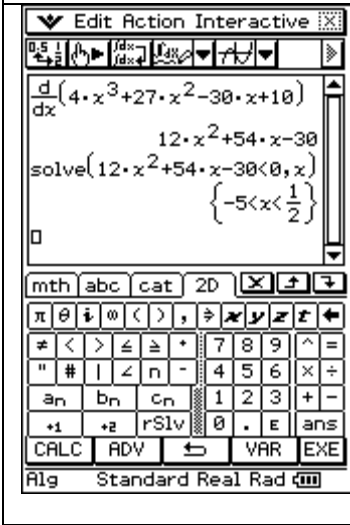

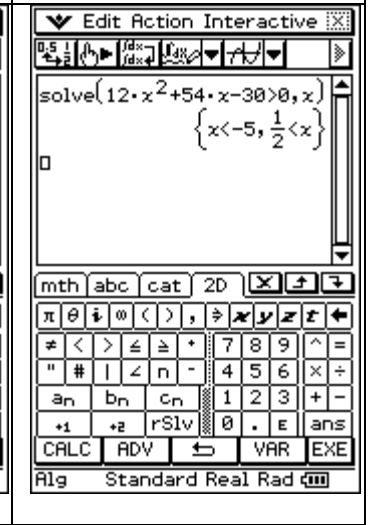
Now interactive  
Calculate  
Diff  
But this time derivative at a point  
Press ok

Answer is 1

Finding the sign of the derivative

How do we calculate when the derivative is negative- positive or zero?

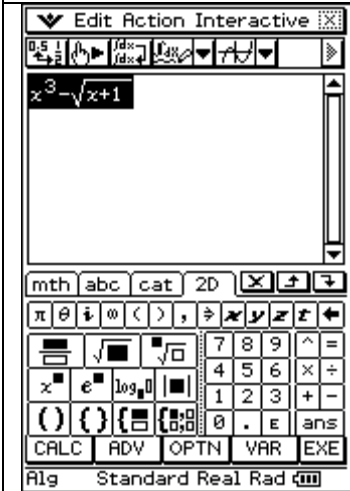
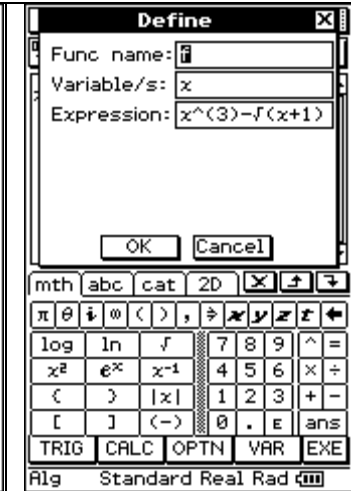
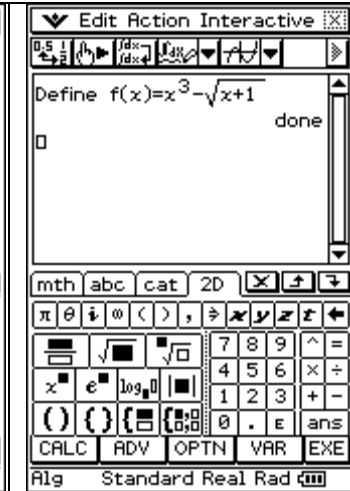
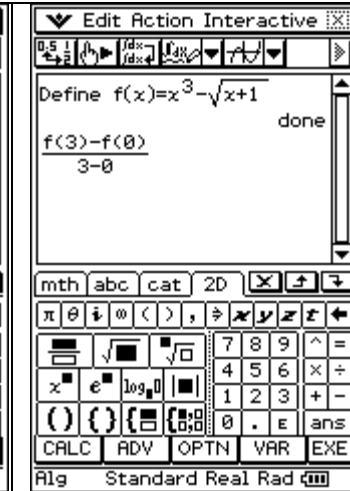
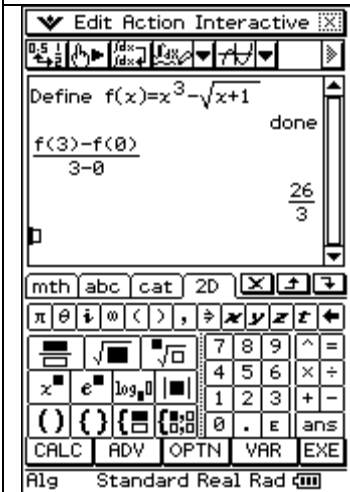
Example: Find when the derivative of  $y = 4x^3 + 27x^2 - 30x + 10$  is negative

			
<p>Put the expression into the main window of the calculator and make sure you highlight it.</p>	<p>Find the derivative first by going to Interactive Calculation Diff Press Ok</p>	<p>We have obtained the derivative</p>	<p>Now select the derivative and Put it on a separate line Make it &lt; 0 Now highlight it</p>
	<p>So the answers are <math>-5 &lt; x &lt; \frac{1}{2}</math></p>		
<p>Now go interactive Equation Solve</p>	<p>Here we see the answers when the derivative is less than zero</p>	<p>What if we wanted to find where the derivative was greater than zero , &gt;0 we would repeat the last step</p>	<p>Go to interactive Equation Solve and you would get the answer</p>

### Finding the average rate of change

How do we calculate the average rate of change of a particular function?


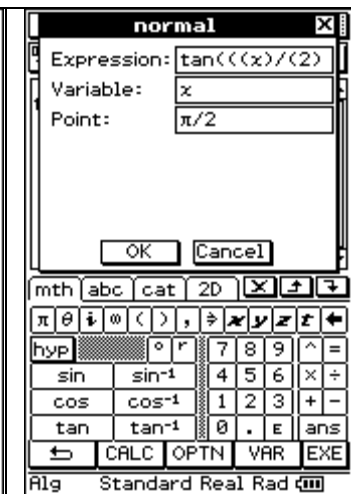
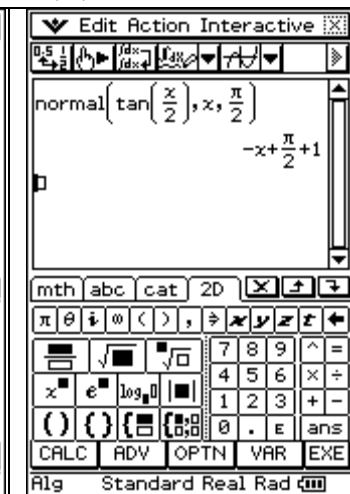
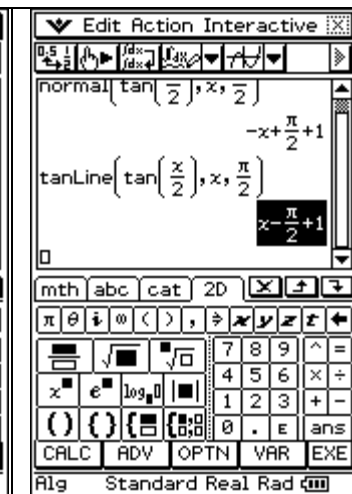
For example find the average rate of change of the function  $f(x) = x^3 - \sqrt{x+1}$  between  $x = 0$  and  $x = 3$

			
<p>Enter the function into the main window. Highlight the function</p>	<p>Tap interactive Define And call it f And press ok</p>	<p>This is what you will see after you press OK</p>	<p>Now enter the expression <math>\frac{f(3) - f(0)}{3 - 0}</math></p>
			
<p>Press Exe and you will see the above So the answer is <math>\frac{26}{3}</math></p>			

## Tangents and Normal's

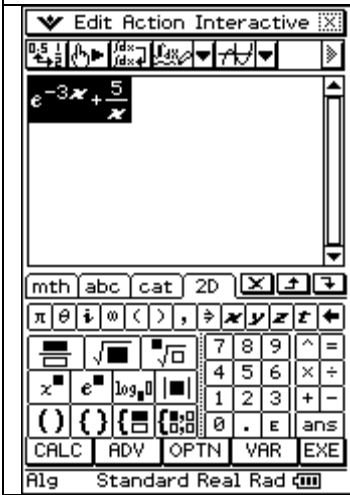
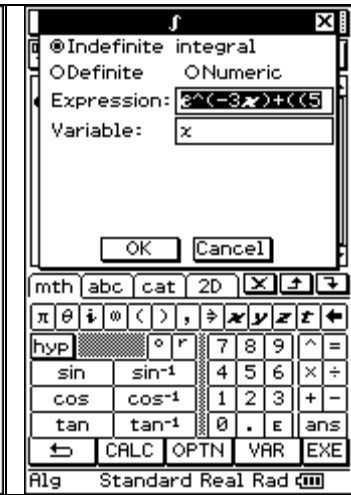
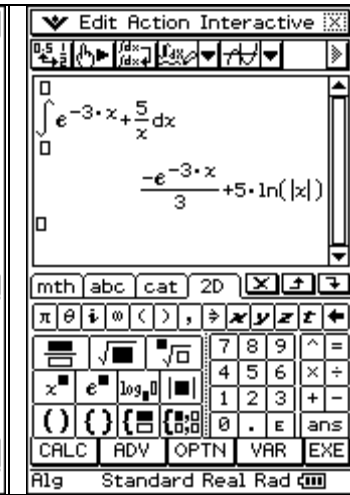
How do we find the equation of the normal or tangent to the graph of a function?

For example: Find the equation of the normal to the graph  $y = \tan\left(\frac{x}{2}\right)$  at the point where  $\frac{\pi}{2}$

			
<p>Enter the equation in the main screen the equation <math>\tan\left(\frac{x}{2}\right)</math></p> <p>And highlight it</p>	<p>Tap interactive Calculation</p> <p>Then Normal</p> <p>And put the point <math>\frac{\pi}{2}</math></p> <p>Press OK</p>	<p>So the equation of the normal is given as <math>y = -x + \frac{\pi}{2} + 1</math></p>	<p>Repeat the entire process but this time use tanline to get the tangent to the line and you will get the above</p>

## Indefinite Integral



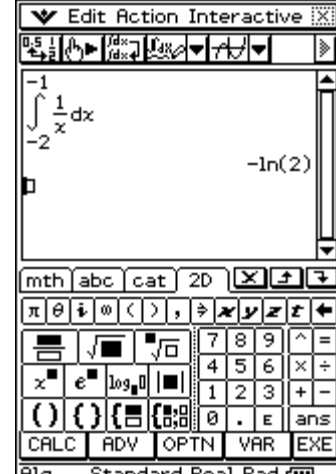
How do we calculate the indefinite integral? For example how do we find the  $\int\left(e^{-3x} + \frac{5}{x}\right)dx$

			
<p>Enter the equation into the main section of the calculator</p> <p>Highlight the equation</p>	<p>Go interactive Calculation</p> <p>The <math>\int</math></p> <p>Now make sure indefinite integral and press OK</p>	<p>And the answer is given</p>	

### Definite Integrals

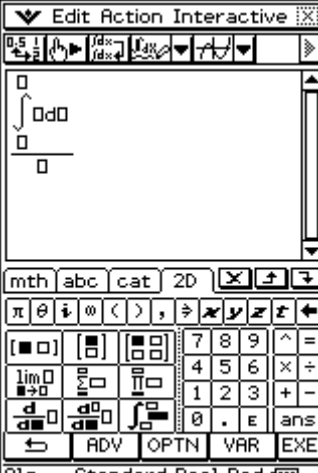
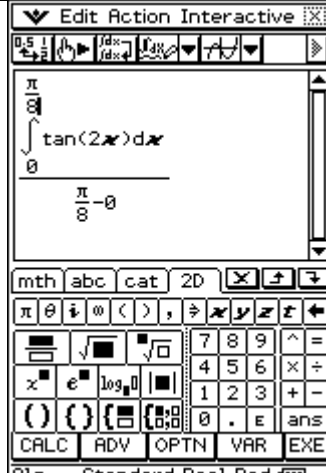
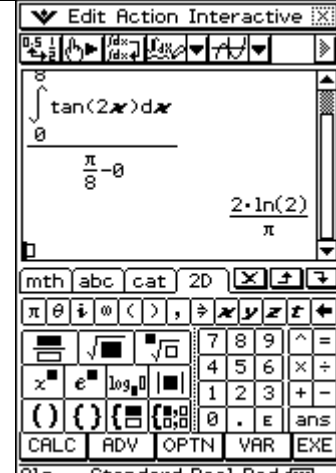
Now we need to find the definite integral.

Find the value of  $\int_{-2}^{-1} \frac{1}{x} dx$

			
<p>Enter the equation into the main area of the calculator and make sure you highlight it</p>	<p>Go interactive Calculation Then <math>\int</math> This time selected definite</p>	<p>Press OK and answer is given</p>	

### Finding the average value of a function over a given interval

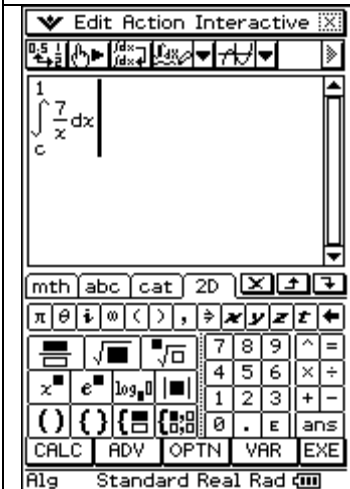
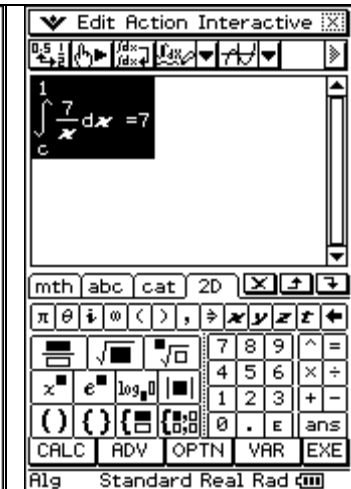
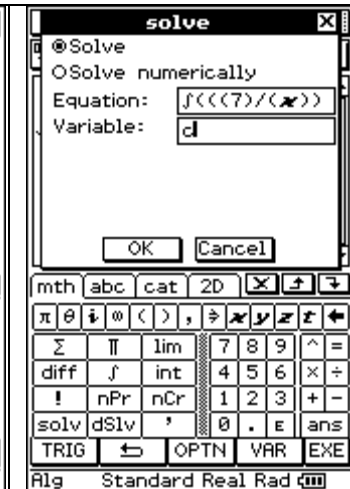
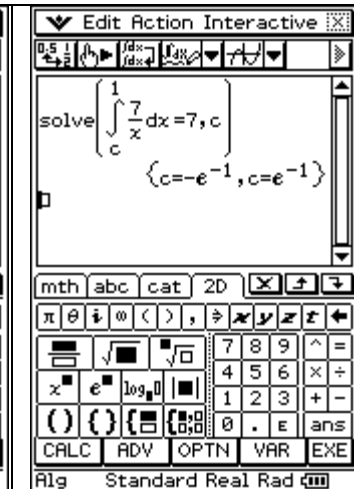
Find the average value of the function  $y = \tan 2x$  over the interval  $\left[0, \frac{\pi}{8}\right]$

			
<p>Put the function into the main area of the calculator using 2D expression First press the division Then enter the integral expression</p>	<p>Now enter the numbers</p>	<p>Now press EXE and answer is given</p>	

## Solving definite equations

Sometimes we need to solve for an unknown in an equation involving a definite integral.

For example : We are asked find the value of c in the following equation  $\int_c^1 \frac{7}{x} dx = 7$

			
<p>Make sure the line is flashing before you put the = 7 otherwise you will not get any solutions IMPORTANT-remember flashing! Cursor and then</p>	<p>Put the equation into main view and then highlight it. <b>Make sure there is a gap between dx and =</b></p>	<p>Go to interactive Equation Solve And make sure you put c for the variable you want.</p>	<p>And we have two solutions. You will need to check the questions to see if both solutions are included.</p>

Definite integration

Let us see how we can find the following:  $\int_1^3 (x^2 - 3x)dx$

<p>We could just put the equation in and press EXE</p>	<p>And we have the answer But sometimes it is better to see the graph of the function</p>	<p>Put the graph into the main screen Then click on the graph button Highlight the equation and drag it into the bottom screen</p>	<p>This is what you will see</p>
<p>Press resize screen</p>	<p>Now you can press Analyse G-Solve Then the integration symbol Press 1  on the keyboard We now enter the values of x</p>	<p>And we get the answer to the integration.</p>	